



**UNIVERSIDAD AUTÓNOMA DE NUEVO LEÓN**  
**FACULTAD DE INGENIERÍA MECÁNICA Y ELÉCTRICA**  
**TIPO DE EXAMEN Y/O EVALUACIÓN:**  
**EXTRAORDINARIO (*Extra Exam*)**

**MATERIA/UNIDAD DE APRENDIZAJE:** *Temas Selectos de Optimización*

**LEARNING UNIT:** Selected Topics on Optimization (in English)

**SEMESTER:** January – June 2026 (Spring)

**ACADEMY:** Statistics and Operations Research (*Estadística e Investigación de Operaciones*).

**INSTRUCTOR:** Dr. Roger Z. Ríos Mercado (ID 090969)

**DIRECTIONS.-** Answer the following questions and/or exercises in the answer sheet. Do not write in this sheet

**SECTION 1: QUESTIONS (50 POINTS)**

Answer and justify your answer.

1. [UT1: Combinatorial optimization; 5 pts] Define a combinatorial optimization problem.
2. [UT1: Combinatorial optimization; 5 pts] Define and explain what a brute-force enumeration method is for solving a combinatorial optimization problem.
3. [UT2: Heuristics; 5 pts] Define and explain what a heuristic method is for solving combinatorial optimization problems.
4. [UT2: Constructive heuristics; 5 pts] What is a constructive heuristic?
5. [UT2: Local search heuristics; 5 pts] Explain clearly what a local search heuristic is for a combinatorial optimization problem.
6. [UT2: Constructive heuristics; 5 pts] Describe in detail the nearest neighbor heuristic for solving the Traveling Salesman Problem. Illustrate your idea with an example or drawing.
7. [UT2: Local search heuristics for the TSP; 5 pts] Describe in detail the nearest insertion heuristic for solving the Traveling Salesman Problem. Illustrate your idea with an example or drawing.
8. [UT1: Combinatorial optimization; 5 pts] Is it true that the Traveling Salesman Problem is hard to solve? Explain.
9. [UT2: Constructive heuristics; 5 pts] Do constructive heuristics guarantee to find a feasible solution to a given combinatorial optimization problem? Justify your answer.
10. [UT2: Local search heuristics; 5 pts] Explain the difference between the “first found” and “best found” strategies employed in local search heuristics.

REVISIÓN No.:7

VIGENTE A PARTIR DE: 01 de Agosto del 2016

## SECTION 2: PROBLEMS (50 POINTS)

1. The  $p$ -Dispersion Problem ( $p$ DP) is defined as follows. Given a collection of points in the plane,  $V = \{1, 2, \dots, n\}$ , where the distance  $d_{ij}$  between every pair of points  $i, j$  in  $V$  is known, and given a known positive integer number  $p$ , the goal is to decide a subset of  $p$  points of  $V$ , in a such a way that these points are as disperse (far away from each other) as possible. In other words, find a subset  $X$  of cardinality  $p$  such that a dispersion objective function is maximized. For a feasible solution given by  $X = \{v_1, v_2, \dots, v_p\}$ , the dispersion function is computed as:

$$f(X) = \sum_{\substack{i, j \in X \\ i < j}} d_{ij}$$

that is, the sum of distances among all pairs of points in subset  $X$ . The problem consists of finding the subset  $X$  that maximizes function  $f(X)$ , that is, that maximizes the sum of pair-wise distances in set  $X$ . In Figure 1 below, there is an instance with 13 points and a corresponding distance matrix  $D$ .

The following questions refer to the  $p$ DP instance described in Figure 1, assuming  $p = 3$ .

- (a) [UT1: Combinatorial optimization; 5 pts] Is  $X^{(1)} = \{3, 6, 9, 11\}$  a feasible solution? Justify your answer.
- (b) [UT1: Combinatorial optimization; 5 pts] Is  $X^{(2)} = \{1, 5, 12\}$  a feasible solution? Justify your answer.
- (c) [UT1: Combinatorial optimization; 8 pts] Among the following three solutions, sort them from best to worst. Justify your answer.  
 $X^{(3)} = \{3, 6, 8\}$ ,  
 $X^{(4)} = \{6, 7\}$ ,  
 $X^{(5)} = \{2, 5, 11\}$ .
- (d) [UT2: Constructive heuristics; 10 pts] Starting from scratch, design a constructive heuristic for finding a feasible solution to the  $p$ DP with  $n$  points and  $p$  dispersion points. Show very clearly and precision each step of your heuristic either in pseudocode or flow chart.
- (e) [UT2: Constructive heuristics; 6 pts] Illustrate how your heuristic works by applying it step by step in the example (Figure 1) to build a feasible solution to the problem. Was this solution better than solution  $X^{(3)}$  from (c)?
- (f) [UT2: Local search heuristics; 10 pts] Given a feasible solution to the  $p$ DP, design a local search for the problem. It is sufficient to describe **very clearly** how you define your move/neighborhood.
- (g) [UT2: Local search heuristics; 6 pts] Illustrate how your local search works starting from the following feasible solution  $X^{(3)} = \{3, 6, 8\}$ . Do at least one **complete** iteration

under the best found strategy showing all computational details. Did the solution improve?

